

A Coupled Leaf/Canopy Turbid Medium Radiative Transfer Model

Barry D. Ganapol Departments of Hydrology and Water Resources and Aerospace and Mechanical Engineering

> University of Arizona 520/621-4728 ganapol@cowboy.ame.arizona.edu









Light is transmitted through the atmosphere and reflected from vegetation canopy elements and background to an air or space borne sensor.

reliably Can the reflected information be, interpreted through the vegetation canopy reflectance? What social implications will the reliable interpretation of reflected information from foliage have?

- Basic Science
 - + Photosynthesis
 - + Establish ecological principles
- Precision Agriculture
 - + Improved crop yield
 - + Improved crop management
- Global climate change prediction
 - + Terrestrial surface reflectance
 - + GCM verification and validation
- Precision Battlefield Engagement (PBE)
 - + Warfighter asset management
 - + Adversary asset strength and location



General CR Modeling Considerations

Vegetation signatures:

- + Spectral λ : Wavelength response of canopy element ($R_{\rm f}, T_{\rm n}, A_b$)
- + Spatial (*x*,*y*): arrangement of scattering objects within canopy
- + Temporal (t): intra- and inter- annual variability
- + Directional (Ω): anisotropy resulting from surface roughness
- + Polarization: (Q): polarized state of surface reflected photons

Factors influencing reflectance:

+ size, shape and distribution of canopy phytoelements
+ biophysical parameters: Leaf Area Index (LAI)



Leaf Area Index (LAI) fAPAR leaf optical properties Leaf Angle Distribution (LAD)

Presentation:

- Focus on turbid medium model LCM2
 - Describe the microscopic leaf radiative transfer model
 - Describe the macroscopic leaf radiative transfer model in the canopy
 - O LCM2 Polarization (LCM2P) algorithm

Demonstrate application of LCM2



General Turbid Medium Canopy Modeling Considerations



Radiative Transfer (RT) considerations:

+ Intra-leaf + Inter-leaf | scattering and absorption

Complicated participating medium

- + Not a well posed **RT** problem
- + Ignorant of biophysical properties and configurations
- + Must rely on natural averaging and a little luck





Typical anatomical structure of a leaf

- + Air-epicuticular wax interface (upper epidermis)
 - thin wax film
 - multilayered membrane of pectin, cellulose, cutin and wax
- + Palisade Parenchyma
- + Spongy Mesophyll
- + Epicuticular wax -air interface (lower epidermis)

Leaf Scattering Phase Function (Microscopic)

+ Microscopic leaf radiative transfer

$$\begin{bmatrix} \Omega \frac{\partial}{\partial \tau} + 1 \end{bmatrix} I(\tau, \Omega; \Omega_0) = \frac{\omega}{4\pi} \int_{4\pi} d\Omega' I(\tau, \Omega'; \Omega_0)$$
$$I(0, \Omega; \Omega_0) = \delta(\Omega - \Omega_0)$$
$$I(\Delta_L, \Omega(-\mu, \phi); \Omega_0) = 0$$



Solution by Siewert's FN Method



Required data: Σ_a and Σ_s -- the scattering and absorption coefficients

+ Calibration of leaf scattering coefficient



HH-R and HH-T: For an isotropic source

$$\rho_{L}(\Sigma_{a},\Sigma_{s}) = \frac{\omega}{2} \sum_{\alpha=0}^{L-1} c_{\alpha} \int_{0}^{1} d\mu \mu \phi_{\alpha}(-\mu) \qquad \tau_{L}(\Sigma_{a},\Sigma_{s}) = E_{2}(\Delta_{L}) + \frac{\omega}{2} \sum_{\alpha=0}^{L-1} d_{\alpha} \int_{0}^{1} d\mu \mu \phi_{\alpha}(\mu)$$
$$\frac{\rho_{L}(\Sigma_{a}',\Sigma_{s};\lambda) = \rho_{EXP}}{\tau_{L}(\Sigma_{a}',\Sigma_{s};\lambda) = \tau_{EXP}} \implies \Sigma_{a}'(\lambda), \Sigma_{s}(\lambda)$$





+ Macroscopic diffuse leaf radiative transfer model

Leaf: Bi-Lambertian diffuse surface phase function



Area scattering phase function (2-angle)

$$\frac{1}{\pi}\Gamma(\Omega',\Omega) = \int_{2\pi} d\Omega_L |\Omega \bullet \Omega_L| g_L(\Omega_L) \gamma_D(\Omega',\Omega;\Omega_L).$$

 $\sim g_L(\Omega_L) =$ Leaf Angle Distribution (LAD)

Area scattering phase function (1-angle) $\Gamma_D(\mu',\mu) \equiv \int_{0}^{2\pi} d\phi \left[\frac{1}{\pi}\Gamma_D(\Omega',\Omega)\right]$

For HH- Reflectance and Transmittance

$$\gamma_{D}(\Omega',\Omega;\Omega_{L}) = \begin{cases} \frac{1}{\pi} \rho_{L}(\lambda) |\Omega \cdot \Omega_{L}|, & (\Omega \cdot \Omega_{L}) (\Omega' \cdot \Omega_{L}) < 0\\ \frac{1}{\pi} \tau_{L}(\lambda) |\Omega \cdot \Omega_{L}|, & (\Omega \cdot \Omega_{L}) (\Omega' \cdot \Omega_{L}) > 0. \end{cases}$$

$$\Gamma_D(\mu',\mu) = 2\int_{-1}^{1} d\omega g_L(\omega) a(\mu',\omega) b(\mu,\omega)$$

Quadrature approximation

$$\Gamma(\mu',\mu) \cong \sum_{m=1}^{Lmc} g_L(\omega_m) c(\mu',\omega_m) d(\mu,\omega_m)$$

Leaf phase function for specular reflection and polarization

+ Specular reflection



$$\gamma_{sp}(\Omega',\Omega;\Omega_L) \equiv K(\kappa,\Omega'\bullet\Omega_L)F_s(n,\Omega'\bullet\Omega_L)\delta_2(\Omega\bullet\Omega_L^*) \qquad K(\kappa,\Omega'\bullet\Omega_L) \equiv e^{-\left[2\kappa\tan(-\Omega'\bullet\Omega)/\pi\right]}$$

Two-angle:
$$\frac{1}{\pi}\Gamma_{sp}(\Omega',\Omega) = \frac{1}{2\pi} \int_{2\pi} d\Omega_L g_L(\Omega_L) |\Omega' \bullet \Omega_L| \gamma_{sp}(\Omega',\Omega;\Omega_L) = \frac{1}{8\pi} g_L(\mu_L^*) K(\kappa,\gamma) F_s(n,\gamma)$$

One-angle: $\Gamma_{sp}(\mu',\mu) = \frac{1}{4\pi} \int_{0}^{\pi} d\omega g_{L}(\mu_{L}^{*}[\cos(\omega)]) K(\kappa,\gamma[\cos(\omega)]) F_{s}(n,\gamma[\cos(\omega)])$

+ Phase function for the linearly polarized component

- -- Experimental evidence indicates that polarization originates predominately at the leaf surface from specular reflection.
- -- Use the vector transport equation to describe the intensity and the linearly polarized component.

Phase function for the linearly polarized component: the mathematical model





Intensity:
$$\rho_s = F_s(n,\gamma) = \frac{1}{2} [\rho_{\rm H} + \rho_{\perp}]$$

 $\rho_{\rm H} = \frac{1}{2} \left[\frac{\sin^2(\gamma - \tilde{\gamma})}{\sin^2(\gamma + \tilde{\gamma})} \right]$
 $\rho_{\perp} = \frac{1}{2} \left[\frac{\tan^2(\gamma - \tilde{\gamma})}{\tan^2(\gamma + \tilde{\gamma})} \right]$
Second Stokes Component: $\rho_Q = F_Q(n,\gamma) = \frac{1}{2} [\rho_{\rm H} - \rho_{\perp}]$

$$\underline{L}(\lambda) = \begin{bmatrix} 1 & 0 \\ 0 & \cos(2\lambda) \end{bmatrix}$$
$$\underline{T}(n,\gamma) = \begin{bmatrix} F_s(n,\gamma) & F_Q(n,\gamma) \\ F_Q(n,\gamma) & F_s(n,\gamma) \end{bmatrix}$$

Phase Function: $\underline{\Gamma}(\mu',\mu) =$

$$=\frac{1}{4\pi}\int_{0}^{\pi}d\omega g_{L}(\mu_{L}^{*})\underline{L}(-\lambda)\bullet$$

• $K(\kappa,\gamma(\Omega'\bullet\Omega))\underline{T}(n,\gamma(\Omega'\bullet\Omega))\underline{L}(\lambda').$

The Radiative Transport Algorithm with Leaf Polarization

The Vector Transport Equation

$$\vec{I}(\tau,\mu) \equiv \begin{bmatrix} I(\tau,\mu) \\ Q(\tau,\mu) \end{bmatrix} \qquad \begin{bmatrix} \mu \underline{I} \frac{\partial}{\partial \tau} + G(\mu) \underline{I} \end{bmatrix} \vec{I}(\tau,\mu) = \int_{-1}^{1} d\mu' \underline{\Gamma}(\mu',\mu) \vec{I}(\tau,\mu') + BC \\ \vec{I}(\tau,\mu) = \vec{I}_{0}(\tau,\mu) + \vec{I}_{c}(\tau,\mu)$$

Uncollided component: $\vec{I}_0(\tau,\mu) = \begin{bmatrix} 1\\ 0 \end{bmatrix} e^{-\tau/\xi} \delta(\mu - \mu_0) \Theta(\tau/\xi) \qquad \xi \equiv \mu/G(\mu)$

Collided component:

$$\begin{bmatrix} \mu \underline{I} \frac{\partial}{\partial \tau} + G(\mu) \underline{I} \end{bmatrix} \vec{I}_{c}(\tau, \mu) =$$

$$= \int_{-1}^{1} d\mu' \underline{\Gamma}(\mu', \mu) \vec{I}_{c}(\tau, \mu') + \underline{\Gamma}(\mu_{0}, \mu) \begin{bmatrix} 1 \\ 0 \end{bmatrix} e^{-\tau/\xi_{0}} \qquad \text{Intercept function:}$$

$$G(\Omega) = \frac{1}{2\pi} \int_{2\pi+1}^{1} d\Omega_{L} |\Omega \bullet \Omega_{L}| g_{L}(\Omega_{L})$$

$$\vec{I}_{c}(0,\mu) = 0$$

$$\vec{I}_{c}(\Delta,-\mu) = 2\rho_{T} \left[\mu_{0}e^{-\tau/\xi_{0}} + \int_{0}^{1} d\mu'\mu' I_{c}(\Delta,\mu') \right] \left[\begin{array}{c} 1\\ p_{T} \end{array} \right] \qquad \text{Degree of polarization of Target}$$

■ The SN/Romberg Algorithm for Intensity



Discretizations:

$$P_{N/2}(\pm \mu_m) = 0, \quad m = 1, N/2$$
$$h \equiv \Delta/N_h$$

Romberg iteration:

$$\int_{h} dx g(x) = \sum_{k=1}^{K} \alpha_{k} g_{k} + O(h^{K})$$
$$I_{c,j,m}^{Exact} = I_{c,j,m} + \sum_{k=2}^{\infty} \beta_{k} h^{k}$$

Numerical implementation and convergence

Evaluation of area scattering phase functions

$$\Gamma(\mu',\mu) = \int_{0}^{\pi} d\omega f(\cos(\omega)) = \sum_{m=1}^{Lmc} \omega_m f_m$$

Iteration Strategy--

- (1) Increment SN order and quadrature order Lmc
- (2) Perform SN sweeps to convergence
- (3) Monitor reflectance and transmittance for both components
- (4) Apply Wynn-epsilon acceleration

$$\varepsilon_{-1}^{(n)} = 0, \quad \varepsilon_{0}^{(n)} = S_{n}$$
$$\varepsilon_{k+1}^{(n)} = \varepsilon_{k}^{(n+1)} + \left[\varepsilon_{k}^{(n+1)} - \varepsilon_{k}^{(n)}\right]^{-1}$$

(5) Go to (1) until (4) converges

• Qualification and Demonstration (Zenith Sun) Comparison of LCM2/LCM2P (LAI = 1, $\rho_T = 0.1$)





Convergence of the W- ε Acceleration (N ₀ = 10)						
Lm	Lmc	W-E	Rfn	Error	Error	
			U	W-E	Rfn	
22	10	3.6810E-02	3.6810E-02	2.6166E+01	1.0000E+00	
24	12	3.6868E-02	3.6868E-02	1.5579E-03	1.5579E-03	
26	14	3.6903E-02	3.6903E-02	9.6828E-04	9.6828E-04	
28	16	3.6927E-02	3.6927E-02	6.5138E-04	6.5138E-04	
30	18	3.6944E-02	3.6944E-02	4.5973E-04	4.5973E-04	
32	20	3.6957E-02	3.6957E-02	3.3706E-04	3.3706E-04	
34	22	3.6966E-02	3.6966E-02	2.5506E-04	2.5506E-04	
36	24	3.6973E-02	3.6973E-02	1.8287E-04	1.8287E-04	
38	26	3.6977E-02	3.6977E-02	1.1872E-04	1.1872E-04	
40	28—	→3.6980E-02 -	→3.6980E-02	6.8486E-05	6.8486E-05	
42	30	3.6981E-02	3.6981E-02	4.2281E-05	4.2281E-05	
44	32	3.6983E-02	3.6983E-02	3.3926E-05	3.3926E-05	
46	34	3.6984E-02	3.6984E-02	3.5482E-05	3.5482E-05	
48	36	3.6986E-02	3.6986E-02	4.0690E-05	4.0690E-05	
50	38	3.6987E-02	3.6987E-02	4.7207E-05	4.7207E-05	
52	40	3.6986E-02	3.6989E-02	4.2763E-05	5.3886E-05	
54	42	3.6989E-02	3.6991E-02	8.0632E-05	4.9856E-05	
56	44 —	→3.6989E-02	3.6992E-02	1.1775E-06	3.0001E-05	
58	46	3.6996E-02	3.6993E-02	1.9800E-04	1.9641E-05	
60	48	3.6989E-02	3.6994E-02	1.9303E-04	1.4928E-05	
62	50	3.6966E-02	3.6994E-02	6.1240E-04	1.4725E-05	
64	52	3.6993E-02	3.6995E-02	7.1229E-04	1.5901E-05	
66	54	3.7002E-02	3.6995E-02	2.6683E-04	1.7624E-05	
68	56	3.6999E-02	3.6996E-02	1.0612E-04	1.4997E-05	
70	58 —	→3.6999E-02	3.6996E-02	3.9680E-07	1.1253E-05	
72	60	3.6999E-02 —	—▶3.6997E-02	1.0864E-06	8.8883E-06	
74	62	3.7000E-02	3.6997E-02	3.1928E-05	8.1139E-06	
76	64	3.6997E-02	3.6997E-02	7.8482E-05	7.8789E-06	
78	66	3.6999E-02	3.6998E-02	4.4057E-05	8.6515E-06	
80	68	3.7000E-02	3.6998E-02	4.2742E-05	7.9577E-06	
82	70	3.7000E-02	3.6998E-02	2.0422E-07	6.2885E-06	
84	72	3.7000E-02	3.6998E-02	7.1298E-07	5.3577E-06	
86	74	3.7000E-02	3.6998E-02	1.0642E-05	4.8736E-06	
88	76	3.7000E-02	3.6999E-02	8.9489E-06	4.7407E-06	
90	78	3.7001E-02	3.6999E-02	1.5724E-05	4.9800E-06	
92	80	3.7001E-02	3.6999E-02	6.6756E-06	4.6481E-06	
94	82	3.7001E-02	3.6999E-02	1.7446E-06	3.8941E-06	
96	84	3.7000E-02	3.6999E-02	2.6794E-05	3.4720E-06	
98	86	3.7001E-02	3.6999E-02	2.3889E-05	3.1392E-06	
100	88	3.7001E-02	3.6999E-02	8.5448E-07	3.1088E-06	
102	90	3.7001E-02	3.7000E-02	1.5302E-06	3.1535E-06	

Table 1 Convergence of the W c Acceleration (N = 1



for an unpolarized target































4 Background Polarizations



MODEL-BASED NEURAL NETWORK ALGORITHM FOR COFFEE RIPENESS PREDICTION USING HELIOS UAV AERIAL IMAGES

R. Furfaro^a, B. Ganapol^a*, L. Johnson^b, S. Herwitz^b

a: Aerospace Mechanical Engineering Dept, University of Arizona, AZ b: NASA AMES Reseach Center, Moffet Field, CA

*: Speaker

SPIE 11th International Symposium Remote Sensing Bruges, 19-22 September 2005

UAVs FOR PRECISION AGRICULTURE:

- UAV: Unpioleted Aerial Vehicle (Air Tower)
- Helios and Pathfinder-plus prototypes
- NASA technology transfer concept
- New way of doing agriculture









NASA COFFEE PROJECT: "The Vision"

- Searching for "heavenly " coffee through UAVs: Helping the farmers to find the best harvesting strategy using remote sensing
- 1st mission for technology proof of concept flew in Oct '02
- Our group is involved in image processing
- **Research and practical issue:** Can we create an intelligent reliable algorithm to predict the percentage of ripe (yellow) cherries in the field?





SOLUTION: Model Based Neural Network

- Design a Neural Network trained to learn the percentage of ripe cherries in the field
- The algorithm is based on a true radiative transport model
- The algorithm is to be put on the **on-board microprocessor** to elaborate airborne images
- Ripe percentages sent to the ground for real-time prediction



MODELING THE RADIATIVE REGIME IN PLANT CANOPIES:LCM2

Goal: generation of a true radiative transport model to simulate the radiative field in vegetation canopies

Approach:

- First principles application: Balance of photons
- Two levels of description: Leaf and Canopy model (nested models)
- **Biochemistry** included as key element affecting vegetation optics
- Connection of the models via leaf optical properties



CANOPY GOVERNING EQUATION

Balance of photons in the phase space: Plane symmetry



Model output: Reflectance at Top of Canopy

$$R_f = \frac{1}{\pi} \int_{2\pi} d\Omega' |\mu| I(0, \Omega'), \mu < 0$$

Leaf/Canopy Model: LCM2 FLOWCHART



Neural Networks (NNs) Overview

- **NNs** are composed by elements operating in parallel. They are biologically inspired to nervous systems
- **NNs** function depends on the way elements are connected
- NNs "learn": Learning can be supervised or not
- NNs applications: Classification, Pattern recognitions, control systems etc.



Model Based NN: Design and Training

• LCM in the forward mode

 $R_{f} = f(D_{ch}, D_{w}, D_{p}, D_{lc}, Sp, LAI, LAD, SR, RC\%, GC\%, YC\%, M\%, \lambda)$

• LCM in the inverse mode

 $[M\%, RC\%, GC\%, YC\%] = f(D_{ch}, D_w, D_p, D_{lc}, Sp, LAI, LAD, SR, R_f, \lambda)$

• Reduced inverse problem: Design issues

How many neurons in the hidden layer? How many points in the training set?

• Neural Network performance:

Learn the training set Generalizes well



- Advantage: Model knowledge allow us to generate as many points as needed
- Disadvantage: Model may not be in the domain of experiment

Training Results and Regression analysis



- Regression analysis: linear fit
- Correlation coefficient **R** = 1
- Perfect fit within 10⁻⁶

- Network Trained in "Batch mode"
- Training goal for the error function 10-7
- Early stopping not observed



Neural Network Performances: Coffee Canopy Simulation Scene

Coffee-Canopy: LCM input parameters							
Chlorophyll	Water	Lignin	Cellulose	LAI	LAD	Sun A	Soil R
37.8 %	6.0e-4	1.2e-3	7.2e-1	0.8	planophile	25 deg	0.3

	Real	NN	Real	NN	Real	NN	Real	NN
Leaf	0.3654	0.3655	0.3603	0.3592	0.2536	0.2533	0.3358	0.3354
Under-ripe	0.1400	0.1398	0.0493	0.0495	0.0721	0.0718	0.0534	0.0533
Ripe	0.0589	0.0588	0.0839	0.0840	0.2920	0.2924	0.3567	0.3572
Over-ripe	0.4357	0.4360	0.5065	0.5073	0.3824	0.3824	0.2541	0.2541
Leaf	0.4983	0.4977	0.2713	0.2711	0.0922	0.0933	0.4516	0.4525
Under-ripe	0.0595	0.0592	0.1614	0.1617	0.4249	0.4246	0.1472	0.1462
Ripe	0.0890	0.0893	0.0287	0.0284	0.1662	0.1661	0.1879	0.1882
Over-ripe	0.3532	0.3538	0.5385	0.5387	0.3168	0.3160	0.2134	0.2131
Leaf	0.4906	0.4904	0.2460	0.2477	0.4433	0.4427	0.2618	0.2623
Under-ripe	0.0712	0.0707	0.3418	0.3409	0.0147	0.0143	0.1663	0.1660
Ripe	0.1750	0.1755	0.1122	0.1120	0.2816	0.2823	0.0877	0.0876
Over-ripe	0.2632	0.2634	0.3001	0.2993	0.2604	0.2607	0.4842	0.4841
Leaf	0.4435	0.4425	0.2280	0.2283	0.0490	0.0494	0.1310	0.1314
Under-ripe	0.0142	0.0140	0.1722	0.1723	0.2861	0.2866	0.2093	0.2093
Ripe Over-	0.2219	0.2225	0.3557	0.3558	0.2512	0.2508	0.4551	0.4552
ripe	0.3204	0.3209	0.2440	0.2436	0.4136	0.4132	0.2047	0.2042



Error Range:

 $10^{-3} \div 10^{-5}$

Neural Networks for Airborne UAV images

- The NN technique is be applied to UAV airborne images
- Images come from the 2002 Kauai (Hawaii) campaign
- UAV images available at three bands: 580, 660 and 790 nm (visible & infrared)
- Fairly cloud-free, atmosphere corrected collages of images
- **DNs-Reflectance** transformation performed at NASA Ames
- Parchment data available
- Missing a-priori information
- Multiple NNs required
- Use Domain Projection Technique



Domain Projection Technique: Overview

- Any NN learns the provided training data set: Extrapolation is unphysical
- Model and measurement errors: Reflectance outside the training set
- **Domain Projection Technique (DPT): Project the reflectance back into domain**
- Marching toward the central point with three different speeds
- Monitor the network output: Stop when results are physical
- Correction technique required



Domain Projection Technique: Application



Multiple NNs and DPT Coupled Algorithm

- Missing a-priori information: 27 neural networks trained
- MATLAB image processing and algorithm implementation performed



Processing the UAV images: Fields and Blocks



NN prediction vs Parchment data & Branch Count

Field 408								
	Under-ripe %	Ripe % (R)	Over-ripe %(O)	R + O %				
Parchment Data	39.45	39.55	21.00	60.55				
Neural Network	36.39	25.10	38.49	63.59				
Branch Count	х	21.14	47.08	68.22				
Error NN %	3.06	14.45	17.49	3.04				
Error Branch %	Х	18.41	26.08	7.67				

Field 406							
	Under-ripe %	Ripe % (R)	Over-ripe %(O)	R + O %			
Parchment Data	52.51	17.30	30.19	47.49			
Neural Network	49.11	20.97	29.90	50.87			
Branch Count	Х	34.33	58.53	92.86			
Error NN %	3.40	3.67	0.29	3.38			
Error Branch %	Х	17.03	28.34	45.37			

Field 410								
	Under-ripe %	Ripe % (R)	Over-ripe %(O)	R + O %				
Parchment Data	71.61	15.14	13.25	28.39				
Neural Network	49.58	17.08	33.33	50.41				
Branch Count	Х	24.07	51.08	75.15				
Error NN %	22.03	1.94	20.08	22.02				
Error Branch %	Х	8.93	37.83	46.76				

NN Ripeness Prediction Maps: Field 408 Block 4









Conclusions

- NASA Coffee Project: Intelligent tool for precision agriculture devised
- Modeling radiative regime within canopies: LCM2 for coffee canopies
- Neural Network approach: Solution of the inverse problem
- Domain Projection Technique developed as remedy to unphysical results
- NN Decision Block coupled with DPT form the backbone of the method
- Application to UAV images shows the potential of the methodology